

Quantitative Analysis of Gas Hydrates Using Raman Spectroscopy

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A calibration protocol to quantify the compositional information of gas hydrates using Raman spectroscopy is proposed. Structure I pure CH₄-, CO₂- and C₂H₆-hydrates in their deuterated and hydrogenated forms with known cage occupancies were investigated by Raman spectroscopy. Raman scattering cross sections of CH₄ in the large and small cages were found to be very similar, but not identical. Some C₂H₆ bands of C₂H₆-hydrate were tentatively reassigned or newly reported and assigned. Our results show that the relative cross sections of guest vibrational modes in the deuterated hydrate are in agreement with those in the hydrogenated hydrate, whereas they are considerably different from those in fluid phase. Using our Raman quantification factors, the relative cage occupancies can now be determined more reliably in CH₄-hydrates. Moreover, with additional assumptions, the absolute cage occupancies, the bulk guest composition and hydration number of pure or mixed gas hydrates become accessible by Raman spectroscopy. © 2013 American Institute of Chemical Engineers AIChE J, 59: 2155–2167, 2013

Keywords: Raman spectroscopy, gas hydrate, methane, carbon dioxide, ethane, quantification factor, cross section, hydration number

Introduction

Gas hydrates are nonstoichiometric crystalline solids containing guest molecules within host cages of H-bonded water molecules.¹ Naturally occurring gas hydrates are stable at relatively low temperature (typically < 285 K) and high pressure (typically > 2 MPa) conditions, and occur frequently in and below continental permafrost as well as in marine environments of continental margins.² The encaged guest molecules interact with the hydrate lattices via van der Waals interactions; the main guest constituent is CH₄ with additions of higher hydrocarbons like C₂H₆, as well as CO₂, N₂ and H₂S. Depending on temperature, pressure, molecular size and guest composition, three common structures are identified: which correspond to different frameworks of water molecules; they are referred to as cubic sI, cubic sII and hexagonal sH. The sI structure is considered to be the most common hydrate structure and comprises two small 5¹² (SC, for short) and six large 5¹²6² (LC) cages per unit cell, formed by 46 water molecules. The sII unit cell consists of 16 small 5¹² and eight large 5¹²6⁴ cages formed by 136 water molecules, and the sH unit cell contains three small 5¹², two medium 4³5⁶6³ and one large 5¹²6⁸ cages formed by 34 water molecules. For a pure hydrate with only one type of small guest molecule like CH₄, C₂H₆ and CO₂, sI hydrate is usually formed at moderate pressures.^{3–6} sII hydrates were observed to coexist metastably with sI CH₄- and CO₂-hydrates.^{7–9} For a mixed hydrate with two or more

types of guests, like a CH₄-C₂H₆ mixture, the hydrate structure may vary with the different composition and/or prevailing *P-T* conditions.^{10–13} CH₄, CO₂ and C₂H₆ occupy both the small and large cages. Being in competition for the SCs and LCs, CO₂ and C₂H₆ partition more favorably into the LCs, while CH₄ fills the SCs.^{11,14,15} Furthermore, large cages are generally almost fully occupied, whereas the occupancy of small cages varies by guest.¹

Natural gas and oil industries have been interested in hydrate research since the 1930s as a consequence of the unwanted hydrate formation in pipelines leading to their complete blockage.¹ This interest has increased recently because of several factors. First, the total amount of hydrate-bound methane in geological deposits is large enough to be of possible interest as a future energy resource, although estimations vary by several-orders of magnitude.^{16–18} Second, since global warming destabilizes continental gas hydrates, liberating the very active greenhouse gas methane, may lead to a considerable positive feedback.¹⁹ Third, realizing that CO₂-hydrate is thermodynamically more stable than CH₄-hydrate, a reduction of the anthropogenic greenhouse gas CO₂ via the storage as solid CO₂-hydrate in a sedimentary gas hydrate reservoir was proposed, while simultaneously recovering hydrocarbons.^{20–22} This technique with a maximum of 64% replacement achieved in a CO₂-CH₄ system without additional constituents could help to resolve environmental issues while recovering a primary source of energy.¹⁴ To apply this idea to a larger scale, a better understanding of the involved gas hydrate formation and dissociation mechanisms is required.

Raman spectroscopy, a nondestructive technique, is one of the most powerful tools to investigate both synthetic and

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natural hydrates at the molecular level.^{23–27} One important feature of confocal Raman spectroscopy is the capability to sample small area with a diameter of a few microns, providing information on the homogeneity of gas hydrates by looking at the individual gas hydrate particles.²⁸ In contrast, nuclear magnetic resonance (NMR) spectroscopy,^{29–31} neutron and X-ray powder diffraction (NPD and XRPD, respectively)^{32–34} usually provide bulk information; the spatial resolution of nuclear magnetic resonance imaging and synchrotron microdiffraction is typically one to two orders of magnitude lower than what is routinely available for confocal Raman spectroscopy. In addition, it is simpler and easier to be accessed, compared with neutron or synchrotron diffraction³⁵ and NMR.^{23,29}

Raman spectroscopy is routinely used in a qualitative analysis of gas hydrates, such as their chemical and structural identification. The vibrational modes of the guests (in terms of position, full width at half maximum (FWHM) and peak area) depend on the local environment of the hosting cages and can often be used to identify structure type and cage preferences. The pioneering Raman spectroscopic work was performed by Anthonsen³⁶ on some halogen gas hydrates in 1974. He found the interactions between guest molecules and the hydrate lattice to be very weak when comparing Raman spectra of guests in gas phase and in hydrate cavities. CH₄-CO₂-H₂O sI hydrates synthesized from CH₄-CO₂-H₂O mixtures forming fluid inclusion in quartz were investigated by Seitz et al.³⁷ They came to two conclusions based on their Raman spectra of CH₄-CO₂-H₂O sI hydrate which were later found to be wrong (1) the assignments of the splitting Raman bands at 2903.5 and 2913 cm⁻¹ as the C–H stretching-mode of CH₄ in SCs and LCs, respectively, (2) the suggestion of CO₂ only occupying the large cages in view of the nondoubling of the Fermi dyad of CO₂. Nakahara et al.³⁸ reported Raman investigation of natural air hydrate containing N₂ and O₂, found in deeper parts of polar ice cores. The composition ratio of N₂-O₂ was determined from the peak areas of their vibrational modes; the peak positions were found to downshift as temperature becomes lower. Assuming that Raman intensities of both H₂O and CO₂ are proportional to their molar fractions, Uchida et al.³⁹ determined for the first time the hydration number (i.e., the number of water molecules per guest atom) of CO₂-hydrate by comparing Raman intensities of H₂O and CO₂ molecules of CO₂-hydrate with those of a CO₂-saturated water solution. Sum et al.²³ reassigned the two distinct Raman lines of CH₄ sI hydrate and systematically studied the applications of Raman for determining structure type, cage occupancies and bulk composition of gas hydrates. The intensity-wise counterintuitive assignment of Raman frequencies to the large and small cages³⁷ were resolved by Subramanian and Sloan¹⁵ by referring to the “loose cage-tight cage” model proposed by Pimentel and Charles.⁴⁰ More recently, *in situ* or time-resolved Raman spectroscopy has provided access to study processes in gas hydrates, such as structural transitions, as well as their formation and dissociation kinetics.^{22,41}

Compositional information, i.e., type and proportion of guest species, the cage occupancies of the various guests and the hydration number, is of primary importance for understanding the physical and physicochemical properties of gas hydrates. ¹³C solid-state NMR is considered as a reliable quantitative method and has been applied to interpret the relative cage occupancies of guest molecules in gas hydrates including CH₄, C₂H₆ and CO₂.^{29–31,42} XRPD is mostly used to provide information on the structure type and unit cell

parameters of gas hydrates; efforts were made to determine the absolute cage occupancies of pure gas hydrates by direct-space methods based on laboratory XRPD⁴³ or by using high-resolution synchrotron XRPD³⁴; this was previously only possible using single crystals, which are not easily available and also not easily handled in the case of gas hydrates. Raman spectroscopy does not directly provide the absolute cage occupancies—at least not without further thermodynamic assumptions.²⁴ Relative cage occupancies, however, can be established straightforwardly: for sI CH₄-hydrate the relative cage occupancies of methane in the LCs and SCs deduced from Raman spectroscopy, obtained under the tacit assumption of identical cross section for CH₄ in both cages, are found to be in reasonable agreement with NMR-results.^{44,45} The results for mixed hydrates are more doubtful as evidenced in the following two publications: Kumar et al.³³ found that the compositional information of sII CH₄-C₂H₆-C₃H₈ hydrate determined by ¹³C magic angle spinning NMR spectroscopy is in agreement with the one obtained from Raman spectroscopy and gas chromatography. In contrast, Wilson et al.⁴⁴ cross-calibrated the cage occupancy ratio of CH₄-CO₂ sI hydrate by Raman and ¹³C NMR spectroscopy and found that the difference was approximately 12% for the one reported sample. A further direct comparison between Raman and NMR or XRPD for the mixed hydrate containing CH₄ and CO₂ molecules appears to be necessary. It appears that Raman spectroscopy cannot be applied to accurately quantify the composition of a mixed hydrate without being calibrated by other techniques; in particular, the Raman cross sections of guests in different environments need to be established quantitatively. This indeed has been attempted by geochemists, which have established Raman spectroscopy as a powerful stand-alone quantification method to determine the bulk composition of gases, such as CH₄, CO₂, N₂, and gas-water mixture in fluid inclusions^{37,46–50} and it is certainly worth considering this large body of work.

Quantitative Raman analysis

The quantitative analysis of Raman spectroscopy is based on Placzek's polarizability theory^{46,51} as given by

$$A_i = I_0 \sigma_i N_i \eta_i \quad (1)$$

where A_i is the integrated peak area (intensity) of a Raman active peak for the species i over a finite range, I_0 is the irradiance on the sample, σ_i is the Raman scattering cross section of i at a certain wavelength of the exciting source, N_i is the number of molecules of i in the irradiated volume, η_i is the instrumental efficiency of the optical and electronic response. Equation 1 relates the intensity of each species (A_i) to the number of molecules present in the scattering volume (N_i). Therefore, it is possible to determine the relative proportion of species by comparing their relative intensities. The molar fraction of a certain species a (x_a) can be derived from rearranging Eq. 1

$$x_a = [A_a / (\sigma_a \eta_a)] / \sum_{i=1}^n [A_i / (\sigma_i \eta_i)] \quad (2)$$

$$= [A_a / F_a] / \sum_{i=1}^n (A_i / F_i) \quad (3)$$

where F_a is the Raman quantification factor (F-factor) of species a , and i refers to all species in the mixture.

Obviously, the accurate determination of the composition of a mixture is possible only if σ and η or F values of all species in the system are accurately known. The Raman cross section is the instrument-independent Raman scattering efficiency representing the property of a molecule in the local environment; it is sensitive to pressure and composition.⁴⁸ To determine the guest composition, the combined factor F is more advantageous than an individual calibration of σ and η for a specific Raman spectrometer.⁵⁰ For a mixture, in the case that spectra of species in the same phase (for gas hydrate, it means structure type) and chamber are acquired at the same time or immediately one after the other, it is reasonable to assume that the instrumental efficiencies of different species are identical.⁴⁶ This is to say, the cross-section ratio of species a and b (σ_a/σ_b) is assumed to be equal to the relative F-factor (F_a/F_b). Seitz et al.³⁷ obtained the molar ratios of CH₄ to CO₂ in a variety of CH₄-CO₂-H₂O mixtures trapped into fluid inclusions using Raman spectroscopy and the results are comparable with the determination by microthermometry. Seitz et al.⁴⁹ investigated the relative Raman F-factor of CH₄ to CO₂ (F_M/F_C) in a CH₄-CO₂ mixture for a wide range of temperatures, pressures and compositions, and found that (1) the variation of F_C/F_M (namely, σ_C/σ_M) with composition is not significant within their analytical uncertainty, and (2) F_C/F_M in an equimolar mixture continuously increases with the increasing pressure up to 10 MPa. This may reflect that molecular interactions could indeed be significant in this pressure interval. They also reported that the relative quantification factors of CH₄ to CO₂ in binary CH₄-CO₂ and ternary CH₄-CO₂-H₂O systems are different.^{37,49} Burke summarized the available σ values for dozens of gas species in fluid phase, and emphasized all these data were calibrated from low-density fluid mixtures.⁴⁸

Considerable efforts have also been made to independently quantify guest compositions for gas hydrates by Raman spectroscopy.^{10,13,22,23,38,52} Assuming the cross sections of species in fluid phase and in hydrate lattices being identical, Sum et al.²³ and Subramanian et al.¹⁰ determined the composition of CH₄-CO₂- and CH₄-C₂H₆-hydrates by experimentally calibrating the ratios F_C/F_M and F_E/F_M in a variety of binary CH₄-CO₂ and CH₄-C₂H₆ mixtures in fluid phase under a certain pressure, respectively. However, they did not investigate the effect of pressure on the relative F-factors. Chazallon et al.⁵² reported the molar proportions of N₂ and O₂ in the N₂-O₂ synthesis hydrate by using the available cross-section values published by Schrötter and Klöckner.⁵¹ Ota et al.²² directly took the value of the relative F-factor of CH₄ to CO₂ given by Sum et al.²³ to determine relative abundance of CH₄ after methane hydrate was replaced by liquid CO₂, although they were under different experimental conditions. The validity of the assumption of transferability of Raman cross section of gas in fluid phase to gas hydrate work remains doubtful, however. First, the chemical environment of guests in fluid phase and in hydrate lattices is apparently different, which may result in a significant difference in Raman scattering cross section. Second, the guest concentration in gas hydrate is very high, for example, 1 m³ methane hydrate contains the same amount molecules as 164 m³ methane at 293 K and 0.1 MPa,¹ and approximately 1 m³ methane at 293 K and 13.2 MPa. Thus, due to the different densities, the relative F-factor of guests in fluid phase calibrated at one certain pressure cannot be used to determine the composition of gas hydrate without further calibration.

Consequently, a quantitative interpretation of a Raman spectrum of a mixed gas hydrate requires the accurate knowledge of the relative quantification factors for each species in hydrate lattice.

In this article, we describe a calibration procedure to quantify the cage occupancies of guest, the bulk guest composition, as well as the hydrate number of gas hydrates using Raman spectroscopy. Peak positions, FWHMs and intensities of pure deuterated sI CO₂-, CH₄- and C₂H₆-hydrates and pure hydrogenated sI CO₂- and CH₄-hydrates were studied. New assignments were tentatively made for some ethane bands in sI C₂H₆-D₂O hydrates, based on the corresponding bands of ethane in fluid phase. Using Placzek's polarizability theory, the relative Raman quantitative factors of CO₂/CH₄, C₂H₆/CH₄, and guests to host molecules in hydrate lattices were experimentally determined by comparing the intensities of the specific Raman peaks of pure sI CO₂-, CH₄- and C₂H₆-hydrates with known composition obtained from synchrotron X-ray powder diffraction. With several assumptions, the empirical F-factors derived from pure sI gas hydrate can be applied for the mixed gas hydrates.

Experimental Methods

Sample preparation and X-ray diffraction

For the Raman calibration work 11 types of pure sI gas hydrates with known formation conditions, the cage occupancies and hydration number were used (see Table 1). The time-space averaged small (θ_S) and large (θ_L) cage occupancies, expressed as the percentage of the occupancy of a given cage with one guest molecule, for deuterated sI C₂H₆-hydrate were obtained by crystallographic Rietveld refinements of powder diffraction data obtained on the hard X-ray beamline BW5, HASYLAB at DESY, Hamburg;³⁴ the θ_S and θ_L cage occupancies of pure sI CO₂- and CH₄-hydrates were obtained from high-resolution powder diffraction data measured on ID31 at ESRF/Grenoble.^{11,53} All cage occupancies together with their least-squares estimated standard deviations are given in Table 1. Considering the composition of sI, the hydration number (n) of sI gas hydrate was determined by

$$n = 46/(6\theta_L + 2\theta_S) \quad (4)$$

A detailed description of the hydrate synthesis and diffraction setups has been given in previous work.^{7,34,53–55} Here, we only briefly summarize the procedures. All hydrate samples were synthesized in a custom-built high-pressure cell by exposing particles of H₂O or D₂O ice Ih to a specific gas at isobaric condition. The ice particles were obtained in an apparatus, in which H₂O or D₂O (purity given as 99.9%) water was sprayed into liquid N₂ to form spherical ice particles with a typical diameter of tens of μ m. To prevent a contamination from atmospheric H₂O, D₂O ice was produced in a glovebox prepurged with N₂. Ice particles were collected into thin-walled Al-cans, and then placed into the pressure cell within a cryostat bath controlled at the desired temperature. Immediately after closing the pressure cell, gas was admitted up to the designated pressure. All pure CH₄ and CO₂ hydrates were formed under isothermal (close to the ice melting point) and isobaric condition, while the bath temperature for C₂H₆ hydrate was later increased above the ice melting point to allow for a more complete conversion of

Table 1. Synthesis Conditions, Cage Occupancies and Hydration Number Established by Synchrotron XRPD for the Gas Hydrates Used

Sample	P/MPa	T/K	D/day	$\theta_s/\%$	$\theta_L/\%$	n
CH ₄ -D ₂ O	3.5	271	21	85.8 ± 1.3 ^a	99.6 ± 1.0 ^a	5.99 ± 0.05 ^a
CH ₄ -D ₂ O	6	271	21	85.6 ± 0.4 ^a	98.9 ± 0.3 ^a	6.02 ± 0.01 ^a
CH ₄ -D ₂ O	10	271	21	87.3 ± 0.8 ^a	100.0 ± 0.5 ^a	5.94 ± 0.02 ^a
CH ₄ -D ₂ O	15	271	21	88.5 ± 0.4 ^a	100.0 ± 0.5 ^a	5.93 ± 0.02 ^a
CH ₄ -H ₂ O	3.5	268	21	85.6 ± 0.4 ^a	98.3 ± 0.3 ^a	6.05 ± 0.01 ^a
CH ₄ -H ₂ O	6	268	21	87.1 ± 0.5 ^a	100.0 ± 0.5 ^a	5.95 ± 0.02 ^a
CH ₄ -H ₂ O	10	268	21	87.0 ± 0.9 ^a	100.0 ± 0.5 ^a	5.95 ± 0.03 ^a
CH ₄ -H ₂ O	15	268	21	85.4 ± 0.4 ^a	100.0 ± 0.5 ^a	5.97 ± 0.02 ^a
CO ₂ -H ₂ O	3	268	21	68.5 ± 0.4 ^b	98.4 ± 0.3 ^b	6.33 ± 0.02 ^b
CO ₂ -D ₂ O	3	271	21	67.4 ± 0.3 ^b	98.9 ± 0.1 ^b	6.32 ± 0.01 ^b
C ₂ H ₆ -D ₂ O	3.8	270 ^d	7 ^d	—	—	—
		278 ^c	14 ^c	4.8 ^c	100 ^c	7.55 ^c

^aCage occupancies are the unpublished values given by Hartmann.

^bData are taken from Hartmann et al.³³

^cData are taken from Murshed et al.³⁴

^dand ^e correspond to the two stages at different temperatures and durations to form sI C₂H₆-D₂O hydrate.

ice particles into gas hydrates; for details see Table 1. The hydrate formation reactions were allowed to proceed typically for several weeks. The reaction was stopped by rapid cooling while concomitantly releasing the pressure, the samples recovered within seconds and transferred to a liquid nitrogen Dewar, where they were stored for subsequent use. Samples for Raman measurements were ground into a size of 200–300 μm , and also stored under liquid N₂.

Apparatus

Raman spectra were acquired by a confocal Raman spectrometer (LabRAM HR800, Horiba Jobin Yvon) equipped with a 600 grooves/mm grating and a Peltier-cooled charge-coupled device detector (DU 420A, Andor, 1024 × 256 pixels). An Ar⁺ laser (Innova 9C, Coherent) emitting a wavelength of 488 nm was used as the excitation source at the output power of 20.5 mW. Measurements were made in confocal configuration by focusing the laser beam via 50× long working distance objective (Numerical aperture = 0.55, Olympus). The backscattered mode was used. The confocal aperture was set to 100 μm . The resulting diameter and the power of laser beam on the focused sample were around 1.1 μm and 4.5 mW, respectively. Each spectrum, collected at a nominal resolution of 2.2 cm^{-1} , was obtained in two accumulations of 30 s exposure time within a range of 100 cm^{-1} to 4000 cm^{-1} . The temperature of the Raman laboratory was controlled to 295 ± 1 K by an air-conditioner.

The Raman analysis was carried out in a cooling and heating stage (Linkam THMS600), which was placed under an Olympus microscope attached to the spectrometer. The device was operated at 113 K with an ambient pressure N₂ atmosphere to prevent gas hydrate decomposition. The precision of the temperature control as well as the stability of temperature during the measurements was ±0.1 K. To calibrate the Raman quantification factors, pure deuterated sI CO₂-, CH₄- and C₂H₆-hydrates were loaded into three separate areas of the cooling chamber; then the samples were measured one after the other. In the same way, pure hydrogenated sI CO₂- and CH₄-hydrates were studied. Three to four sets of spectra were recorded for each loading, and three loadings were made. The temporal interval between two consecutive Raman measurements of the separated samples of one loading was typically 4–6 min.

Because of a possible nonlinearity of the spectrometer, peak position was calibrated against three emission lines of a

mercury lamp (in air) at 2179.30, 3159.61 and 3222.64 cm^{-1} . Emission lines were recorded simultaneously with the Raman spectra of samples, rather than measured before or after each sample measurement, as shown in Figure 1. In principle, this procedure allows for a better accuracy in determining the peak positions while simplifying the measurement procedures. The estimated uncertainty obtained from the reproducibility of peak position determined by this method is better than ±0.8 cm^{-1} . After the baseline correction, each spectrum was fitted in the region of interest by a Gaussian/Lorentzian mixed function using “dmfit” software.⁵⁶ The Gaussian/Lorentzian ratio y ($yG/(1-y)L$) was established for each peak and then kept constant during further analysis. Raman spectral parameters, such as peak position, FWHM and the integrated area, were determined.

Results and Discussion

Methane hydrate

CH₄-D₂O and CH₄-H₂O sI hydrates formed at 6 MPa were chosen for the investigation of the Raman peak positions and FWHMs, as listed in Table 2; the uncertainties as obtained from the reproducibility are shown. Four bands of CH₄ molecules encaged into the deuterated or hydrogenated

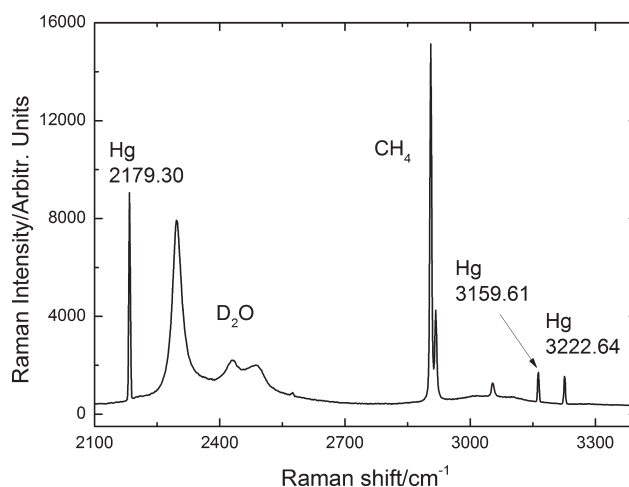


Figure 1. A representative Raman spectrum showing the bands of CH₄-D₂O hydrate and three emission lines of mercury recorded simultaneously.

Table 2. Assignments, Gaussian/Lorentzian Ratio y ($yG/(1-y)L$), Peak Positions and Full Width at Half Maximums (FWHMs) of Raman Bands of the Deuterated and Hydrogenated sI CH₄-Hydrates Formed at 6 MPa Measured at 113K under Atmospheric Pressure of N₂

Assign.	Cage	y	sI CH ₄ -D ₂ O hydrate		sI CH ₄ -H ₂ O hydrate	
			ν/cm^{-1}	FWHM/ cm^{-1}	ν/cm^{-1}	FWHM/ cm^{-1}
$2\nu_4$	—	0.0	2570.3 ± 0.5	4.8 ± 0.9	2569.8 ± 0.2	4.4 ± 0.5
ν_1	5^{12}	0.6	2901.6 ± 0.1	4.8 ± 0.3	2901.3 ± 0.2	5.0 ± 0.2
ν_1	$5^{12}6^2$	0.45	2913.4 ± 0.2	5.5 ± 0.3	2913.0 ± 0.1	6.3 ± 0.4
$2\nu_2$	—	0.0	3050.1 ± 0.2	7.5 ± 0.4	3048.9 ± 0.4	9.4 ± 0.5

sI hydrate were observed, as illustrated in Figure 2. Two strong distinct peaks at 2901.3 cm^{-1} and 2913.0 cm^{-1} are related to the totally symmetric C—H stretching mode (ν_1)²³ of CH₄ in the LCs and SCs of the hydrogenated framework, respectively, while the ν_1 bands arising from CH₄ trapped into the LCs and SCs of the deuterated hydrate lattices are located at 2901.6 and 2913.4 cm^{-1} , respectively. The widths of ν_1 bands of CH₄ in the hydrogen-bonded water cages are slightly bigger than those in the deuterated cages. Compared with the corresponding excitation obtained in the gas phase with only one band $\approx 2917.1 \text{ cm}^{-1}$,⁵⁷ the band splits and both resulting bands are redshifted highlighting the change of the methane molecules' particular chemical environment. The published values for the ν_1 vibration of CH₄ given by different authors vary from 2901.2 to 2905 cm^{-1} for CH₄ in LC and from 2913.6 to 2916 cm^{-1} in SC of sI CH₄-hydrate.^{11,23,25,58,59} The differences may be due to different temperatures and pressures during the data collection. The peak positions reported here are close to the values given by Ohno et al.⁵⁸ obtained at 95 K in a nitrogen atmosphere using laser light at a wavelength of 632.8 nm. Mangir and Kuhs¹¹ found that positions of the ν_1 bands of sI CH₄-hydrate shift to higher wave numbers by less than 1 cm^{-1} when temperature increases from 113 K to 173 K, however, no investigation has been made on the temperature dependence of the band positions of sI CH₄-hydrate at higher temperature. Moreover, Lu et al.⁵⁷ reported that Raman frequency of methane in vapor phase changes as a simple function of vapor density. It could imply that the ν_1 bands of CH₄ molecules in sI CH₄-hydrate also vary with the different cage occupancies. A broader band at 3048.9 and 3050.1 cm^{-1} is the overtone of C—H asymmetric bending mode ($2\nu_2$) of methane included in the hydrogenated and deuterated hydrate, respectively. It is approximately $3\text{--}4 \text{ cm}^{-1}$ lower than the previous data.^{11,27,60} Another minor peak at 2570.3 cm^{-1} , superimposed by the broad O—D stretching mode of D₂O framework, and at 2569.8 cm^{-1} is the first overtone of the C—H bending mode ($2\nu_4$) of CH₄ enclathrated in the deuterated and hydrogenated hydrate lattices, respectively. Chazallon et al.²⁷ gave the similar peak position of $2\nu_4$ band under the similar measurement conditions.

The cage occupancy ratio reflecting the distribution of CH₄ molecules in the large and small cages is generally determined by directly comparing peak areas of the two ν_1 bands of CH₄ included in sI hydrate lattices. In this study, the intensities of the C—H stretching mode of CH₄ enclathrated in the LCs and SCs of sI hydrogenated and deuterated hydrates formed at different pressures, A_{ML} and A_{MS} , were integrated within the range of $2830\text{--}3000 \text{ cm}^{-1}$. As mentioned previously, for sI gas hydrates the number of the large cages is three times that of the small cages. The cage occupancy ratio of CH₄ can be obtained by

$$\theta_{ML}/\theta_{MS} = A_{ML}/3\sigma_{ML} / (A_{ML}/\sigma_{MS}) \quad (5)$$

$$\approx A_{ML}/3A_{MS} \quad (6)$$

where θ_{ML} , θ_{MS} and σ_{ML} , σ_{MS} are the absolute fractional occupancies and the Raman scattering cross sections of methane molecules in the large and small cages, respectively. Assuming σ_{ML} and σ_{MS} to be identical, Eq. 6 was used to determine cage occupancy ratio of CH₄ and the hydration number in sI methane hydrate.^{23,24} However, the different cage sizes can be assumed to cause slightly different C—H bond lengths of CH₄ in the LCs and SCs; consequently, the Raman scattering cross sections of CH₄ in two cages can be expected to be somewhat different.^{25,61}

To elucidate the possibly slightly different Raman scattering cross sections for CH₄ in small and large cages, the θ_{ML}/θ_{MS} ratios of deuterated and hydrogenated sI CH₄-hydrates, synthesized at different P - T conditions, were cross-calibrated by our synchrotron X-ray powder diffraction and Raman data obtained for the same samples. The cage fillings, established straightforwardly from diffraction data with a precision of typically better than 1% (see Table 1), together with a similar precision of the Raman intensity measurements allow us for the first time to proceed; the $\theta_{ML}^R/\theta_{MS}^R$ ratios were computed using Eq. 6 and are given in Table 3 with their standard deviations for the measured data. It can be seen that the ratios determined by synchrotron powder diffraction measurements $\theta_{ML}^D/\theta_{MS}^D$ are generally slightly higher than those from Raman spectroscopy $\theta_{ML}^R/\theta_{MS}^R$, but still comparable. Relying on the absolute values obtained from diffraction, the relative Raman scattering cross sections $\sigma_{ML}^R/\sigma_{MS}^R$ can be calculated using Eq. 5 with uncertainties

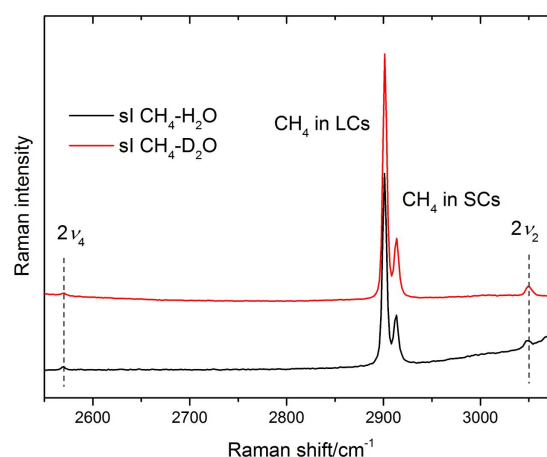


Figure 2. Typical Raman spectra of deuterated and hydrogenated sI CH₄-hydrates measured at ambient pressure and 113 K.

[Color figure can be viewed in the online issue, which is available at [wileyonlinelibrary.com](http://www.wileyonlinelibrary.com).]

Table 3. Relative Cage Occupancies and Raman Scattering Cross Sections of sI CH₄-D₂O and CH₄-H₂O Hydrate Determined by Synchrotron XRPD and Raman Measurements

Sample	T/K	P/MPa	$\theta_{ML}^D/\theta_{MS}^D$	$\theta_{ML}^R/\theta_{MS}^R$	$\sigma_{ML}^R/\sigma_{MS}^R$
CH ₄ -D ₂ O	271	3.5	1.16 ± 0.02	1.148 ± 0.014	0.989 ± 0.012
CH ₄ -D ₂ O	271	6	1.16 ± 0.01	1.125 ± 0.011	0.974 ± 0.009
CH ₄ -D ₂ O	271	10	1.15 ± 0.01	1.100 ± 0.023	0.960 ± 0.020
CH ₄ -D ₂ O	271	15	1.13 ± 0.01	1.077 ± 0.020	0.953 ± 0.019
CH ₄ -H ₂ O	268	3.5	1.15 ± 0.01	1.150 ± 0.017	1.002 ± 0.015
CH ₄ -H ₂ O	268	6	1.16 ± 0.03	1.135 ± 0.026	0.977 ± 0.022
CH ₄ -H ₂ O	268	10	1.15 ± 0.01	1.110 ± 0.024	0.965 ± 0.021
CH ₄ -H ₂ O	268	15	1.17 ± 0.01	1.102 ± 0.021	0.941 ± 0.018

^D and ^R indicate diffraction and Raman methods, respectively.

obtained from error propagation. The relative cage occupancies derived from Raman scattering for both H₂O and D₂O hydrates appear to decrease as the synthesis pressure increases from 3.5 to 15 MPa; the reason for this behavior is not entirely clear, however, a possible explanation is a pressure-dependent (i.e., cage-filling dependent) change of the relative size of the SCs and LCs⁶² with a corresponding slight change of relative cross section. As it can be seen from Table 3, the relative cross sections of CH₄ in the small and large cages for sI deuterated and hydrogenated hydrates formed under the same experimental conditions are not significantly different.

The average value of sI CH₄-H₂O and CH₄-D₂O hydrates formed at pressures from 3.5 to 15 MPa is 0.974 ± 0.028 . The error is the standard deviation from the mean of totally 120 measurements. Undoubtedly, the Raman scattering cross section of CH₄ in 5¹²⁶ cages is close to that in 5¹² cages, but they are not identical. It is the first time to experimentally confirm the difference of the Raman scattering cross sections of CH₄ encaged into the large and small cages of sI CH₄-hydrate predicted by Tulk.²⁵ Therefore, to obtain the accurate values predicted by Raman spectroscopy, such as the cage occupancy ratio, and with further thermodynamic assumptions,^{23,24} the hydration number of sI CH₄-hydrate, the determined should be used as a correction factor.

Carbon dioxide hydrate

In Figure 3, one characteristic doublet, also known as Fermi dyad, was observed at 1277.6 and 1382.8 cm⁻¹ for sI CO₂-D₂O hydrate, and 1275.5 and 1379.4 cm⁻¹ for sI CO₂-H₂O hydrate. These two respective bands correspond to the lower (ν_{c-}) and upper (ν_{c+}) levels of Fermi resonance resulting from two vibrational modes with nearly the same energy: the symmetric stretching vibration ν_1 and the overtone of the bending modes $2\nu_2$ of CO₂ molecules trapped into hydrate cavities. These two modes perturb each other in the excited states through Fermi resonance. The peak positions of Fermi bands in H₂O hydrate host are considerably lower than in the D₂O framework, see Table 4. In addition, the ν_{c-} band of CO₂-D₂O hydrate is almost twice as broad as that of CO₂-H₂O hydrate. Our results of CO₂ bands in H₂O lattices are on the lower side of the published data, which vary in a range of 1274–1278 cm⁻¹ and 1377–1384 cm⁻¹.^{23,39,63,64} As discussed earlier, CO₂ molecules occupancy both the LCs and SCs,^{42,65} but Raman bands of CO₂ between the LCs and SCs are overlapping and cannot be resolved in this study. A weaker peak around 1368.4 cm⁻¹ for CO₂-D₂O hydrate and 1366.6 cm⁻¹ for CO₂-H₂O hydrate is related to the isotopic splitting of ¹³CO₂ referring to the previous assignments for ¹³CO₂ in vapor phase.⁶⁶ The large uncertainty shows this

peak is difficult to be resolved due to its weakness and overlap with the upper Fermi dyad.

Ethane hydrate

Raman spectra of C₂H₆ are more complex due to the molecules' six Raman-active fundamental modes, many overtones and combinations as described by Helvoort et al.⁶⁷ Raman spectra of the C—C and C—H stretching vibrations of ethane trapped into hydrate lattices have been studied to determine hydrate structure type and to estimate the composition of ethane or mixed hydrate.^{10,11,23,26,68,69} However, the quantitative analysis has not yet been well understood, mainly because the ambiguous assignments of some bands in the C—H stretching region and the low intensity of the C—C stretching mode of ethane in 5¹² cages. The assignments, frequencies, FWHMs and normalized intensities of bands of ethane molecules encaged into sI deuterated hydrate and comparison with ethane bands in fluid phase are given in Table 5. Ethane hydrate was measured at 113 K and under atmospheric pressure of N₂. In this study, by referring to the assignments of ethane in fluid phase given by Helvoort et al.⁶⁷ and Domingo and Montero,⁷⁰ some ethane bands of sI C₂H₆ hydrate were assigned as the corresponding vibrational modes of ethane molecules in the LCs; other peaks were assigned as ethane in the SCs.

Raman spectrum of sI C₂H₆-D₂O hydrate in the ranges of 950–1570 and 2635–3000 cm⁻¹ is illustrated in Figure 4.

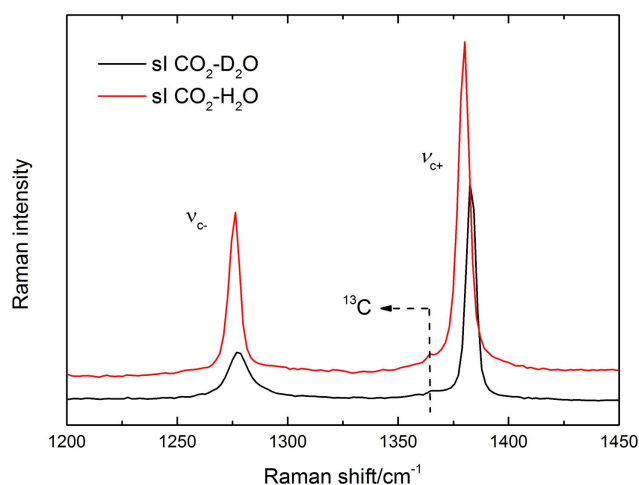


Figure 3. Representative Raman spectra of CO₂ in sI CO₂ hydrates measured at 113 K and ambient pressure.

[Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

Table 4. Assignments, Gaussian/Lorentzian Ratio (y), Peak Positions and FWHMs of Raman Bands of the Deuterated and Hydrogenated sI CO₂-Hydrates Formed at 3 MPa, Measured at 113 K under Atmospheric Pressure of N₂

Assign.	y	sI CO ₂ -D ₂ O hydrate		sI CO ₂ -H ₂ O hydrate	
		ν/cm^{-1}	FWHM/ cm^{-1}	ν/cm^{-1}	FWHM/ cm^{-1}
$\nu_{\text{e-}}$	0.0	1277.6 ± 0.5	11.7 ± 0.4	1275.5 ± 0.8	6.0 ± 0.3
—	0.0	1368.4 ± 1.3	15.9 ± 2.3	1366.6 ± 4.0	14.7 ± 4.0
$\nu_{\text{e+}}$	0.51	1382.8 ± 0.5	5.3 ± 0.3	1379.4 ± 0.8	6.1 ± 0.2

Five peaks exist in the low-frequency region, see Figure 4a. The band at 999.4 cm^{-1} is related to the ¹²C-¹²C symmetric stretching mode (ν_3) of ethane molecules trapped in LCs, whereas on the right shoulder, a much weaker peak at approximately 1019.1 cm^{-1} is associated with the ν_3 vibration of ethane in SCs. The ν_3 band of C₂H₆ enclathrated in LCs of sI and sII hydrates is well defined with a difference of $\approx 8 \text{ cm}^{-1}$,¹¹ this band is a very robust indicator of the structure type of gas hydrate containing ethane molecules. In the current study, it is difficult to accurately quantify the intensity ratio of ethane in the LCs to SCs using the ν_3 band because of its low-intensity resulting from the very low occupancy of ethane in SCs, see Table 5. In addition, another weak peak at 983.2 cm^{-1} originating from the ¹³C-¹²C stretching vibration in LCs indicates small quantity of ¹³C is present in the studied hydrate. These peak positions obtained by the new calibration and fitting procedure are less than 3 cm^{-1} lower than our previous work.¹¹ The other two peaks at 1460.2 and 1546.9 cm^{-1} arising from the CH₃ deformation vibration (ν_{11})⁷¹ and the combination of $\nu_5 + \nu_{12}$ modes of ethane in the LCs, respectively, are reported here for the first time.

In the high-frequency range, Raman spectra of sI C₂H₆-hydrate are more complicated than those of methane hydrate in the same region (see Figure 2) as a consequence of the strong multiple vibrational resonances of ethane molecules occurring among the totally symmetric C—H stretching vibration ν_1 , the asymmetric CH₃—deformation overtones ($2\nu_{11}$ and $2\nu_8$), and their combinations.⁷⁰ The prominent twin bands resulting from a Fermi resonance at 2888.2 and 2942.5 cm^{-1} and an intermediate shoulder around 2924.5 cm^{-1} are assigned to the lower ($\nu_{\text{e-}}$), upper ($\nu_{\text{e+}}$), and intermediate (ν_{ei}) bands of the mixture of $\nu_1:2\nu_{11}:2\nu_8$ vibrational modes of ethane in the LCs, respectively. Hirai et al.⁶⁹ and

Subramanian et al.¹⁰ gave different assignments for these three bands. One broad peak at about 2966.86 cm^{-1} is tentatively assigned as $\nu_{\text{e+}}$ modes of ethane in the SCs. This peak was seen in spectra of pure sI C₂H₆ hydrates in our earlier work, but not discussed; it is noteworthy that the corresponding peak in the sII CH₄-C₂H₆ hydrates formed from a mixture of 95 mol % CH₄ and 5 mol % C₂H₆ is not observed, likely due to the low molar fraction of ethane in the mixed hydrate.¹¹ A newly observed peak at approximately 2952.6 cm^{-1} is more ambiguous due to being superimposed by $\nu_{\text{e+}}$ bands. It could be related to the ν_{10} asymmetric CH-stretching mode of ethane in the LCs. Another more ambiguous peak at approximately 2907.0 cm^{-1} is associated with the $\nu_{\text{e-}}$ mode of ethane in the SCs; the experimental uncertainty here is higher than the usual $\pm 0.8 \text{ cm}^{-1}$, mainly as a result of its low intensity and overlap with other peaks. Following the same calibration procedure for sI methane hydrate, the Raman cross-section ratios of ethane in the LCs and SCs are calculated by

$$\sigma_{\text{EL}}^{\text{R}}/\sigma_{\text{ES}}^{\text{R}} = A_{\text{EL}}^{\text{R}}/3A_{\text{ES}}^{\text{R}}/(\theta_{\text{EL}}^{\text{D}}/\theta_{\text{ES}}^{\text{D}}) \quad (7)$$

Where $\theta_{\text{EL}}^{\text{D}}/\theta_{\text{ES}}^{\text{D}}$ is the cage occupancy ratio of sI ethane hydrate listed in Table 1. The determined $\sigma_{\text{EL}}^{\text{R}}/\sigma_{\text{ES}}^{\text{R}}$ ratios for the $\nu_{\text{e-}}$ and $\nu_{\text{e+}}$ bands are 0.154 ± 0.018 and 0.035 ± 0.003 , respectively. These results suggest that the local environment dramatically affects the $\nu_{\text{e-}}$ and $\nu_{\text{e+}}$ vibrational modes of ethane molecules in the SCs due to the rather small size of 5¹² cages for ethane with a resulting change of the C—H bond length. A much weaker doublet observed at 2735.2 and 2768.5 cm^{-1} can be assigned to $2\nu_6$ and $2\nu_2$ overtones even though they have a slight resonance with ν_1 , respectively, as shown in Figure 4b.⁷⁰ The combination vibration $\nu_{11} + \nu_{12}$ can potentially contribute to the appearance of peak at

Table 5. Assignments, Gaussian/Lorentzian Ratio (y), Raman Shifts, FWHMs and the Normalized Peak Areas of the Observed Bands of C₂H₆ Encaged into the Deuterated sI Hydrate and Comparison with C₂H₆ in Fluid Phase

Assign.	Cage	y	$\nu_{\text{h}}/\text{cm}^{-1}$	FWHM/ cm^{-1}	$R/\%$	$\nu_{\text{f}}/\text{cm}^{-1}$	$\Delta\nu/\text{cm}^{-1}$
—	5 ¹² 6 ²	0.0	983.2 ± 0.8	6.5 ± 2.0	0.4 ± 0.1	—	—
ν_3	5 ¹² 6 ²	0.17	999.4 ± 0.0	4.0 ± 0.2	8.6 ± 1.1	992.5^{a}	+6.9
—	5 ¹²	0.0	1019.1 ± 1.1	15.6 ± 4.3	0.7 ± 0.2	—	+25.6
ν_{11}	5 ¹² 6 ²	0.0	1460.2 ± 0.0	19.4 ± 1.4	8.3 ± 0.4	1468.4^{b}	−8.2
$\nu_5 + \nu_{12}$	5 ¹² 6 ²	0.54	1546.9 ± 0.1	4.2 ± 0.4	0.2 ± 0.0	—	—
$\nu_{11} + \nu_{12}$	5 ¹² 6 ²	0.72	2642.5 ± 0.9	44.1 ± 10.9	1.3 ± 0.4	2658.7^{b}	−16.2
$2\nu_6$	5 ¹² 6 ²	0.66	2735.2 ± 0.0	4.4 ± 0.2	2.4 ± 0.1	2756.5^{c}	−21.3
$2\nu_2$	5 ¹² 6 ²	0.91	2768.5 ± 0.0	5.7 ± 0.1	1.1 ± 0.0	2788.7^{c}	−20.2
$\nu_{\text{e-}}$	5 ¹² 6 ²	0.35	2887.2 ± 0.0	8.6 ± 0.1	25.5 ± 0.4	2896.7^{c}	−9.5
—	5 ¹²	1.0	2907.0 ± 3.4	31.1 ± 3.3	2.7 ± 0.3	—	+10.3
ν_{ei}	5 ¹² 6 ²	0.0	2924.5 ± 0.2	7.4 ± 0.8	3.2 ± 0.4	2938.8^{c}	−14.3
$\nu_{\text{e+}}$	5 ¹² 6 ²	0.35	2942.5 ± 0.0	7.0 ± 0.2	26.9 ± 0.9	2954.8^{c}	−12.3
$\nu_{\text{e+}}$	5 ¹²	1	2966.9 ± 0.0	12.3 ± 0.6	12.2 ± 0.9	—	+12.1
ν_{10}	5 ¹² 6 ²	0.0	2952.6 ± 0.3	20 ± 1.4	6.6 ± 0.7	2968.7^{c}	−16.1

ν_{h} and ν_{f} indicate Raman frequencies of ethane in hydrate lattices and fluid phase, respectively. R is percentage of peak area. ^a, ^b and ^c represent the values given by Helvoort et al.⁶⁷, Fernandez and Montero⁷¹, and Domingo and Montero⁷⁰, respectively. $\Delta\nu$ is the difference between ν_{h} and ν_{f} .

Table 6. Results of the Experimentally Determined Ratios of F-factors of CO₂ and C₂H₆ with Respect to CH₄ in D₂O or H₂O Hydrate Lattices and Comparison with the Established Values in Fluid Phase

F_E/F_M	C ₂ H ₆		F_C/F_M	CO ₂		
	sI C ₂ H ₆ -D ₂ O	Fluid		sI CO ₂ -D ₂ O	sI CO ₂ -H ₂ O	Fluid
F_{999}/F_{2901}	0.21 ± 0.03	0.21 ^a	F_{1278}/F_{2913}	0.13 ± 0.01	0.13 ± 0.01	0.13 ^b
F_{2887}/F_{2901}	0.63 ± 0.03	—	F_{1383}/F_{2913}	0.24 ± 0.02	0.26 ± 0.02	0.2 ^b , 0.34 ^d
F_{2907}/F_{2913}	4.14 ± 0.55	—	F_{CT}/F_{2913}	0.37 ± 0.03	0.39 ± 0.04	0.77 ^c
F_{2942}/F_{2901}	0.67 ± 0.04	1.76 ^b				
F_{2967}/F_{2913}	18.81 ± 1.68	—				
F_{ET}/F_{2901}	1.38 ± 0.07	2.2 ^c				

^aThe value quoted from Schröter and Klöckner⁵¹ was converted using the Eq. 1 in the reference⁴⁸;

^bratios of F-factor were calculated by the given cross sections⁴⁸;

^cand ^e are estimations from the graph in Subramanian et al.¹⁰ and Sum et al.²³, respectively; ^ddata are taken from the Seitz et al.³⁷; F_{ET} and F_{CT} represent the Raman quantification factors were calculated by the sum area of the ν_{e-} , ν_{ei} and ν_{e+} bands of C₂H₆ in the LCs and Fermi diad of CO₂, respectively.

2642.5 cm⁻¹. These three peaks are reported for the first time for ethane in the hydrate phase.

The difference between the band positions of C₂H₆ in sI ethane hydrate (ν_h) and in fluid phase (ν_f), $\Delta\nu = \nu_f - \nu_h$, are also listed in Table 5. It can be seen that $\Delta\nu$'s for ethane in the SCs are all positive, and those in the LCs are negative, except for the C—C vibrational band. Using the semiempirical “loose cage-tight cage” model, Subramanian and Sloan¹⁵ also elucidated that, compared with the corresponding band positions of C₂H₆ in vapor phase, the ν_3 band positions of ethane in LCs and SCs of sI ethane hydrate have a smaller

(6.5 cm⁻¹) and larger (25.6 cm⁻¹) positive Raman shift, respectively, whereas the ν_{e-} and ν_{e+} bands of ethane in LCs show a negative shift. Our results are consistent with their report.

Raman spectra of the hydrate framework

Raman bands of the deuterated framework of sI gas hydrates can be separated into two main regions: the D₂O translational (100–400 cm⁻¹) and the O—D stretching (2100–2830 cm⁻¹) regions, while those of the hydrogenated host can be classified into H₂O translational and the O—H stretching (2830–3600 cm⁻¹) vibrations. In this work, only the O—D and O—H stretching bands of host molecules were considered to calibrate the relative F-factors of different guest molecules. Figure 5 shows Raman spectra of pure sI deuterated hydrates of CO₂, C₂H₆ and CH₄ in the O—D stretching region and sI hydrogenated hydrates of CO₂, and CH₄ in the O—H stretching region. It can be seen that shapes of these bands measured at 113 K under ambient pressure of N₂ are quite similar. Schicks et al.⁵⁹ found that Raman peaks in the O—H stretching range are similar between the pure H₂O ice I_h and sI CH₄-hydrate, whereas they are clearly different for sII CH₄-hydrate. Uras-Aytemiz and coworkers⁷² analyzed aerosols of gas hydrates nanoparticles by FTIR spectroscopy and showed

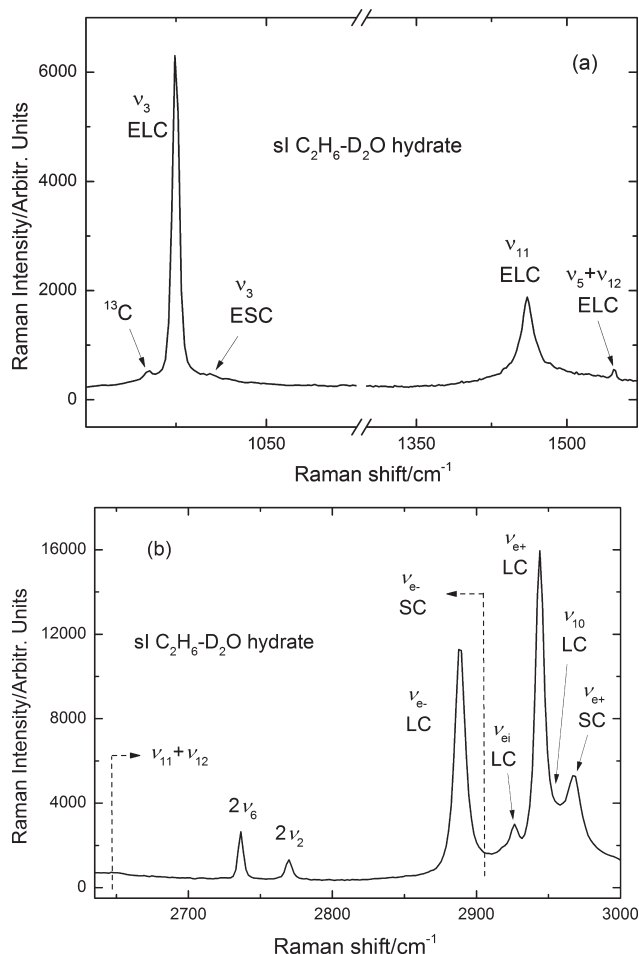


Figure 4. Typical Raman spectra of sI C₂H₆-D₂O hydrate in the range (a) 950–1570 cm⁻¹, and (b) 2635–3000 cm⁻¹.

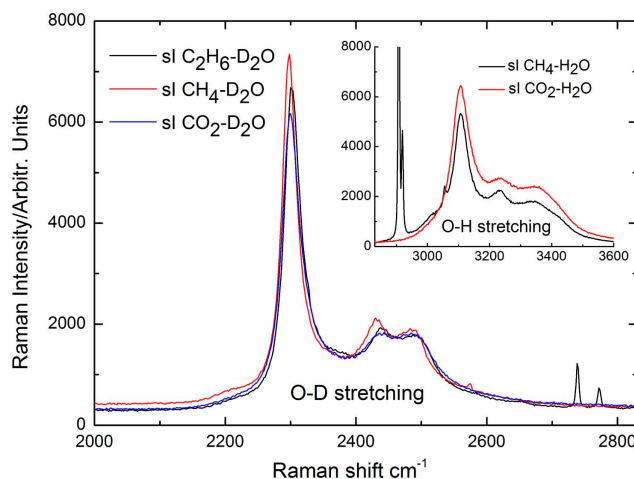


Figure 5. Typical Raman spectra of the O-D stretching vibrational bands of pure deuterated sI CO₂-, C₂H₆- and CH₄-hydrates and the O-H stretching vibrational bands of pure hydrogenated sI CO₂- and CH₄-hydrates (inset).

[Color figure can be viewed in the online issue, which is available at wileyonlinelibrary.com.]

the good agreement of spectra of the D₂O or H₂O frameworks of different deuterated or hydrogenated gas hydrates containing CO₂, CH₄, C₂H₂, etc. The similarity of these spectra suggests that the influence of guest–host interactions onto Raman O—D and O—H stretching vibrations is small. Consequently, the assumption is made in the following that the O—D and O—H stretching Raman signals of host lattices are independent of guest molecules investigated here, which makes them suitable as an internal calibrant for the amount of hydrate in the beam if no ice I_h is present.

Raman quantification factor

In this study, the relative Raman quantification factors of gas hydrates are given in two ways: guest to guest and guest to host framework. Ratios of F-factors of the specific vibrational modes of the trapped CO₂ and C₂H₆ molecules to CH₄ in sI hydrates, F_C/F_M and F_E/F_M , were determined by comparing the spectra of CH₄-hydrate with two consecutive measurements of CO₂- and C₂H₆-hydrates. Peak areas of this set of different spectra are comparable following the experimental procedure discussed above section. On the other hand, the relative F-factor of guest to D₂O or H₂O host, F/F^H , was directly calculated by the corresponding intensities of peaks within the same spectrum. Pure sI CH₄-hydrates formed at 6 MPa, CO₂-hydrates synthesized at 3.5 MPa and C₂H₆-D₂O hydrate synthesized at 3.8 MPa were used for this purpose (see Table 1).

According to Eq. 1, the integrated area of O—D stretching bands of D₂O hydrate is proportional to the number of D₂O molecules in the sampled volume; the same argument also holds for H₂O hydrate. Under the assumption that Raman spectra of host molecules in pure sI CO₂-, CH₄- and C₂H₆-hydrates are independent of the guest species, two scaling factors are introduced

$$C_{CM} = A_C^H/A_M^H \quad (8)$$

$$C_{EM} = A_E^H/A_M^H \quad (9)$$

where C_{CM} refers to the scaling factor of CO₂ to CH₄, C_{EM} is the scaling factor between C₂H₆ and CH₄, A_C^H , A_M^H and A_E^H represent the integration area of the O—D stretching modes of host molecules in 2100–2830 cm^{−1} or those of O—H bands in 2830–3600 cm^{−1}, respectively. By comparing these two factors, the same amount of host molecules as in sI CH₄ hydrate as in two almost concomitant measurements of sI CO₂- and C₂H₆-hydrates are derived. As a result, F_C/F_M and F_E/F_M can be obtained from pure CO₂-, CH₄- and C₂H₆-hydrates with the cage fillings established from synchrotron powder diffraction (see Table 1).

As demonstrated earlier, Raman spectra of CH₄ and C₂H₆ molecules trapped into the LCs and SCs of sI hydrate cavities are both well-defined, while CO₂ cannot be resolved in this study. The relative F-factors of the bands resulting from C₂H₆ in the LCs or SCs to the ν_1 bands of CH₄ in the LCs or SCs are given by the following expressions

$$F_{EL}/F_{ML} = \frac{(A_{EL}/A_{ML})/(\theta_{EL}/\theta_{ML})}{C_{EM}} \quad (10)$$

$$F_{ES}/F_{MS} = (A_{ES}/A_{MS})/(\theta_{ES}/\theta_{MS})/C_{EM} \quad (11)$$

Considering that Raman bands of the encaged CO₂ molecules in the LCs and SCs cannot be resolved, the nontrivial

Table 7. Results of the Experimentally Determined Ratios of F-factors of Guests to Host Molecules in the Deuterated or Hydrogenated sI CH₄-, CO₂- and C₂H₆-Hydrates

Hydrate	F/F^H	Framework	
		D ₂ O	H ₂ O
sI CH ₄	F_{2901}/F_M^H	1.12 ± 0.04	0.95 ± 0.06
	F_{2913}/F_M^H	1.13 ± 0.04	1.03 ± 0.07
sI CO ₂	F_{1278}/F_C^H	0.15 ± 0.01	0.12 ± 0.01
	F_{1383}/F_C^H	0.27 ± 0.03	0.25 ± 0.02
	F_{CT}/F_C^H	0.42 ± 0.04	0.38 ± 0.02
sI C ₂ H ₆	F_{2887}/F_E^H	0.71 ± 0.03	—
	F_{2907}/F_E^H	4.66 ± 0.57	—
	F_{2942}/F_E^H	0.75 ± 0.04	—
	F_{2967}/F_E^H	21.17 ± 1.67	—

F^H refers to the Raman quantification factor of the O—D or O—H stretching-vibrational bands of the host molecules.

assumption is made that the Raman cross sections of CO₂ in the LCs and SCs are identical. F_C/F_M can be obtained by

$$F_C/F_{MS} = A_C / \left(\frac{A_{ML} \times \theta_{CL}}{\theta_{ML} \times \sigma_{ML} / \sigma_{MS}} + \frac{A_{MS} \times \theta_{CS}}{\theta_{MS}} \right) / C_{CM} \quad (12)$$

where σ_{ML}/σ_{MS} is 0.977 for sI CH₄-H₂O, and 0.974 for sI CH₄-D₂O hydrate, see Table 3.

Results of F_C/F_M and F_E/F_M are listed in Table 6. It can be seen that Raman quantification factors of ν_{e-} , ν_{ei} and ν_{e+} bands of C₂H₆ encaged into sI D₂O hydrate are apparently different. Domingo and Montero⁷⁰ also reported the different cross sections of these three bands of C₂H₆ in gas phase. Intensities of peaks centered at 2887.2 and 2942.5 cm^{−1} or the sum of 2887.2, 2952.6 and 2942.5 cm^{−1} are suggested reflecting the molar fraction of C₂H₆ in the LCs, because the uncertainty of their F-factors based on all the measurements are within ±6%, see Table 6. Area ratios of A_{2967}/A_{2913} and A_{2907}/A_{2913} can be used to determine composition of the SCs. The relative F-factor of CO₂ to CH₄, F_C/F_M , derived from H₂O and D₂O host frameworks are identical for ν_{e-} band, and slightly different for ν_{e+} band. This may mean that ratios of F-factors are assumed to be independent of the isotopic composition of the hydrate framework. Consequently, the empirical F_E/F_M obtained by pure sI deuterated C₂H₆- and CH₄-hydrates can also be applied for the sI hydrogenated gas hydrates in good approximation.

It is interesting to compare these results in the hydrate phase with the published F-factors of guests in the fluid phase. As shown in Table 6, the relative F-factors relating the ν_{e-} band of CO₂ in H₂O and D₂O hydrates to the stretching-vibrational peaks of CH₄ in the LCs and SCs of H₂O and D₂O hydrates, F_{1278}/F_{2913} , are identical to the corresponding ratio of CO₂ to CH₄ in the vapor phase, whereas ratio of F-factors of the ν_{e+} bands to CH₄ in the LCs and SCs are up to 30% higher than values published by Burke⁴⁸ and 30% lower than given by Seitz.³⁷ The estimated F_{CT}/F_M (C_T means the sum of the Fermi dyad) from the graph given by Sum et al.²³ is almost two times higher than our result. The relative F-factor relating the C—C stretching band of C₂H₆ to CH₄ in LCs agrees with the result of C₂H₆ and CH₄ in gas phase,⁵¹ even though the uncertainty of our result is larger than 10%. However, a considerable discrepancy occurs for the C—H stretching region of C₂H₆. Comparing the sum of peak areas of ν_{e-} , ν_{ei} and ν_{e+} of C₂H₆ (A_{ET}) with ν_1 band of CH₄ in gas phase, Subramanian et al.¹⁰ reported F_{ET}/F_M to be around 2.2 (estimation from the given

Table 8. The Cage Occupancies of Guests in the LCs and SCs, and Total Cage Occupancies of Guests Trapped into the Deuterated sI CO₂-C₂H₆-CH₄ Hydrate Calculated with the Empirical F-factors

Cage	$\theta_C/\%$	$\theta_M/\%$	$\theta_E/\%$
5 ¹² 6 ²	—	35.9 ± 1.3	24.1 ± 1.3
5 ¹²	—	69.3 ± 2.5	1.0 ± 0.0
Total	26.3 ± 1.7	44.3 ± 1.6	18.3 ± 1.0

graph). It is approximately 60% higher than our result for sI gas hydrates. The ratio of Raman scattering cross sections of ν_{e+} band of C₂H₆ to CH₄ in gas phase given by Burke⁴⁸ is approximately 2.6 times higher than our determination. It can be concluded that the previous assumption that Raman scattering cross section of species keeps constant when free molecules in fluid phase are encaged into the hydrate cavities are an oversimplification.^{10,23}

Using the ratios of Raman quantification factors between guests, the relative abundance of guests in different cages and bulk composition of guests in the mixed gas hydrates containing CH₄, CO₂ and C₂H₆ can be determined. On the other hand, the absolute cage occupancies and bulk composition of gas hydrate can be derived from the relative F-factor of guest to host framework. Comparing peak area of the O—D or O—H stretching-vibrational bands of D₂O or H₂O host framework with the splitting bands of CH₄ or C₂H₆ molecules in different cages of pure sI CH₄- or C₂H₆-hydrate, the relative F-factors of CH₄ or C₂H₆ in the LCs and SCs to host molecules are obtained by

$$F_L/F^H = A_L \times 46 / (A^H \times 6 \times \theta_L) \quad (13)$$

$$F_S/F^H = A_S \times 46 / (A^H \times 2 \times \theta_S) \quad (14)$$

respectively, where 46, 6 and 2 are the number of H₂O or D₂O molecules, the large and small cages per unit cell of sI gas hydrate. For pure sI CO₂-hydrate F_C/F_C^H , is calculated by

$$F_C/F_C^H = A_C/A_C^H \times 46 / (6 \times \theta_{CL} + 2 \times \theta_{CS}) \quad (15)$$

The determined results are shown in Table 7. It can be seen that for pure sI CH₄- and CO₂- hydrates, the relative F-factors in D₂O framework are 8–25% higher than those in H₂O framework. The difference between the cross sections of the same guest molecules in D₂O hydrates cavities and those in H₂O cavities was experimentally established for the first time.

Our calibration strategy provides a workable approach which appears to be more realistic for gas hydrates than the previous methodology, and is expected to deliver more accurate results. To accurately determine the compositional information of gas hydrates, a calibration protocol for the relative Raman quantification factor as proposed in this study should be considered, instead of applying the available cross sections or ratios of F-factor of guests in fluid phase. In addition, the results are also helpful for a better understanding of the interactions of guests and host framework. It should be noted that the cross sections of guests may vary with cage occupancy and guest composition, both possibly mediated by the resulting slight change in the host framework geometry. In this study, the relative Raman quantification factor are

calibrated by one set of gas hydrates with known cage occupancies; further work is needed to study the dependency of the relative Raman scattering cross sections for gas hydrates with different cage fillings.

Application

The relative Raman quantification factors obtained in this study can be used to determine the compositional information of the synthetic and natural sI gas hydrates containing CH₄, CO₂ and/or C₂H₆ in terms of the cage occupancies, the guest composition and hydration number, etc. In particular, for *in situ* Raman investigation on CH₄-hydrate replaced by CO₂ molecules, F_C/F_M and F_C/F_C^H can be applied to infer the local replacement ratio. As mentioned previously, the Raman scattering cross section ratio of CH₄ in the LCs and SCs of sI CH₄ hydrate is close to 1, while the LC/SC ratio of the ν_{e+} band of C₂H₆ in sI hydrate is down to 0.035. This implies that the difference between the cage size and guest molecule size sometimes plays an important role in determining the Raman quantification factor of guest. However, considering the variation of cage size between sI and sII hydrates, the difference for the cross section of CH₄ in a sII structure is not expected to be substantially bigger than the 2–3% difference between methane in the small and large cage in a sI structure. For larger molecules, CO₂ and C₂H₆, the cross section difference may be larger between sI and sII hydrates. Thus, for the price of an additional uncertainty of the F-factor ratio of 5–10%, our results can also be applied to sII CO₂ and C₂H₆ hydrates. Please note, that considering the very high sensitivity of the ethane Raman cross section in the small cage, intercomparisons of the ethane cage occupancies in sII hydrates should be restricted to the large cages.

To apply the empirical Raman quantification factors derived from the comparison of the Raman spectra of pure sI gas hydrates to the mixed system, three assumptions are made:

1. The interactions between guests and the host framework, and among the weakly polar guests located in neighboring cages, such as CH₄, CO₂ or C₂H₆, are small enough to be negligible.
2. The relative Raman quantification factors are independent of the cage occupancies and composition of guests as mediated by the host framework.
3. No ice exists in the system.

While assumption 1 is usually considered acceptable, assumption 2 is not trivial as the water framework and the resulting cage geometry will be affected by variations of cage occupancies and guest type. According to our neutron or X-ray powder diffraction results, the content of pure ice in the clathrate material produced in our laboratory is quite small going up to a few wt %.⁷³ Clearly, it is important to determine the concentration of pure ice in the specific gas hydrates under investigation (e.g., by diffraction) before empirical F-factors are applied.

Figure 6 shows one Raman spectrum of sI deuterated hydrate containing CH₄-CO₂-C₂H₆ mixture with unknown composition. Using the determined F-factors between guest and host molecules, the absolute cage occupancies in 5¹²6² (θ_L) and 5¹² cages (θ_S), and the total cage occupancies of CH₄ or C₂H₆ (θ) are determined by the following expressions

$$\theta_L = A_L \times 46 / (A^H \times 6) / (F_L/F^H) \quad (16)$$

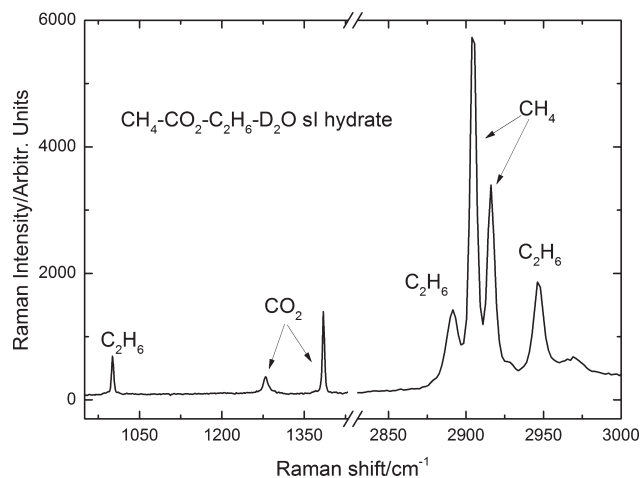


Figure 6. Raman spectra of the deuterated sI CH₄-CO₂-C₂H₆-hydrate measured at ambient pressure and 113 K.

$$\theta_S = A_S \times 46 / (A^H \times 2) / (F_S / F^H) \quad (17)$$

$$\theta = (\theta_L \times 6 + \theta_S \times 2) / 8 \quad (18)$$

while the total cage occupancy of CO₂ (θ_C) is calculated by

$$\theta_C = A_C \times 46 / (A_C^H \times F_C / F_C^H) / 8 \quad (19)$$

The relative F-factors presented in this work (Table 7), F_{2901}/F_M^H , F_{2913}/F_M^H , F_{2942}/F_E^H , F_{2967}/F_E^H , F_{1278}/F_M^H and their corresponding intensities of Raman bands were used to determine the cage occupancies of sI deuterated CH₄-CO₂-C₂H₆-hydrate, see Table 8. The uncertainty of the cage occupancies arises from the uncertainty of the relative F-factors. Not unexpected, but established here in a quantitative manner, methane occupies both the small and large cages, whereas ethane prefers to reside in the LCs. The total cage occupancy of CH₄, C₂H₆ and CO₂ is 88.5 ± 4.3 in percentage, and the bulk guest composition is around $50.0 \pm 1.3\%$ mol CH₄, $20.6 \pm 0.5\%$ mol C₂H₆ and $29.4 \pm 1.8\%$ mol CO₂. Therefore, the calculated hydration number is 6.50 ± 0.25 using Eq. 4. The estimated uncertainty in the hydration number is less than 4%, which permits to establish the composition of the mixed hydrates with useful precision.

Conclusion

Raman spectroscopy is a standard method for the qualitative and semiquantitative analyses of gas hydrates in chemical engineering applications. With some additional calibration effort, it is also a promising useful tool for providing the quantitative information of pure and mixed gas hydrates as demonstrated here for the calibration of Raman quantification factor of guests in the deuterated and hydrogenated sI CO₂-, CH₄- and C₂H₆-hydrates on the basis of the guest molecules' specific Raman bands.

The Raman scattering cross sections of CH₄ molecules enclathrated into 5¹² and 5¹²6² cages are found to be different by directly comparing the analysis of Raman spectroscopy with the absolute cage fillings established by synchrotron X-ray powder diffraction; the difference is small but significant. This slight difference should be taken into consideration for the future determination of the hydration

number of methane hydrate. To proceed in the case of ethane hydrate, we have tentatively assigned Raman bands as ethane molecules trapped into the LCs and SCs by a comparison with the corresponding lines of ethane in fluid phase.

The relative Raman quantification factors of guest to guest and guest to host molecules, were obtained by analyzing the specific peak areas of pure sI CO₂-, CH₄- and C₂H₆-hydrates with known cage occupancies obtained from synchrotron powder diffraction. Our results are considered to be more accurate than the available values of guests calibrated in fluid phase. Under several assumptions, the empirical F-factors can be used for the quantitative analysis of the mixed gas hydrates containing CO₂-, CH₄- and C₂H₆.

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